

- **QUESTION 1**

For the matrix  $A = \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix}$  and the matrix  $B = \begin{bmatrix} 2 \\ 1 \end{bmatrix}$ , find if the expression  $3 - B^T A B$  is positive or negative.

- **QUESTION 2**

Calculate the result of the addition

$$\frac{1-i}{1+i} + \frac{2i}{2+3i}$$

where  $i$  is the imaginary unit.

- **QUESTION 3**

For the matrix  $A = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$  and the vector  $\vec{b} = \begin{bmatrix} 8 \\ -2 \end{bmatrix}$ , find the measure(length) and the angle with respect to the horizontal axis  $x$  of the vector  $\vec{c} = 5\vec{j} + A\vec{b}$ .

- **QUESTION 4**

Find the value of  $\theta$ , when  $\sin(8\theta) \cos(4\theta) = 0$

- **QUESTION 5**

Find the value of  $\theta$ , when  $\tan(5 + \theta) = \tan(5)$

- **QUESTION 6**

Find the first derivative of  $f(x) = \sin(3x^2) + e^x \cdot 3^{-x}$

- **QUESTION 7**

Find the first derivative of  $f(x) = \frac{\sin(3x^2)}{2+\sin(x)}$

- **QUESTION 8**

Find the first derivative of  $f(x) = \frac{\tan(3+x^2)}{e^{2x}}$

- **QUESTION 9**

Find the angle between the vectors  $\vec{a} = \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$  and  $\vec{b} = \begin{bmatrix} 1 \\ -1 \\ 1 \end{bmatrix}$

- **QUESTION 10**

Find the roots of the equation  $\begin{vmatrix} \cos(\theta) & \sin(2\theta) \\ \frac{1}{2} & \cos(\theta) \end{vmatrix} = 0$

- **QUESTION 11**

Calculate the integral  $\int_1^2 x \ln(x^2) dx$

- **QUESTION 12**

Calculate the integral  $\int_2^3 x^2 \ln(x^3) dx$